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| QF01/0408-4.0E | Course Plan for Bachelor program - Study Plan Development and Updating Procedures/ Mathematics Department |
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|----------------|---|---|---|---|---|---|
| Study plan No. | 2021/2022 | | University Specialization | | Bachelor of Mathematics | |
| Course No. | 0101433 | | Course name | | Differential Geometry | |
| Credit Hours | 3 | | Prerequisite/ Co-requisite | | Calculus (3) | |
| Course type | <input type="checkbox"/> MANDATORY UNIVERSITY REQUIREMENT | <input type="checkbox"/> UNIVERSITY ELECTIVE REQUIREMENTS | <input type="checkbox"/> FACULTY MANDATORY REQUIREMENT | <input type="checkbox"/> Support course family requirements | <input type="checkbox"/> Mandatory requirements | <input checked="" type="checkbox"/> Elective requirements |
| Teaching style | <input type="checkbox"/> Full online learning | | <input checked="" type="checkbox"/> Blended learning | | <input type="checkbox"/> Traditional learning | |
| Teaching model | <input type="checkbox"/> 1 Synchronous: 1 asynchronous | | <input checked="" type="checkbox"/> 1 face to face : 1 asynchronous | | <input type="checkbox"/> 2 Traditional | |

Faculty member and study divisions' information (to be filled in each semester by the subject instructor)

| Name | Academic rank | Office No. | Phone No. | E-mail | |
|-----------------|---------------|------------|--------------------|----------------|----------------|
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| Division number | Time | Place | Number of students | Teaching style | Approved model |
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Brief description

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| Plane and space curves, Reparametrization by arc length, Curvature, Torsion, Frenet formulas, Osculating plane, normal plane, Rectifying plane, Bertrand curves, Surfaces in three dimensions, Smooth surfaces, The first fundamental form, length of curves on surfaces, Surface area, The Gauss map, The second fundamental form, Gauss formula, The normal and geodesic curvatures, Principal curvatures, Mean and Gauss curvatures, Geodesics and applications. |
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Learning resources

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|--|--|-------------------------------|--|---------------------------------|--|
| Course book information (Title, author, date of issue, publisher ... etc) | 1) Banchoff, T. and Lovett, S. (2010), Differential Geometry of Curves and Surfaces, USA, A. K. Peters, Ltd., Taylor and Francis Group, LLC. 2) O' Neill, B. (2006), Elementary Differential Geometry, 2 nd edition, USA, Elsevier Inc. | | | | |
| Supportive learning resources (Books, databases, periodicals, software, applications, others) | 1. Pressely, A. (2010), Elementary Differential Geometry, 2 nd edition, London, Springer – Verlage, Springer Undergraduate Mathematics Series. 2. Gray, A., Abbena, E. and Salamon, S. (2006), Modern Differential Geometry of Curves and Surfaces with Mathematica, 3 rd edition, USA, Chapman & Hall/CRC, Studies in Advanced Mathematics, Boca Raton. 3. Kühnel, W. (2006), Differential Geometry, Curves-Surfaces-Manifolds, 2 nd edition, USA, AMS. | | | | |
| Supporting websites | <ul style="list-style-type: none"> • http://en.wikipedia.org/wiki/Differential_geometry • http://ocw.mit.edu/courses/mathematics/18-950-differential-geometry-fall-2008/# • http://www.trillia.com/online-math/geometry.html • http://people.math.gatech.edu/~ghomi/LectureNotes/ | | | | |
| The physical environment for | <input checked="" type="checkbox"/> Class room | <input type="checkbox"/> labs | <input checked="" type="checkbox"/> Virtual educational platform | <input type="checkbox"/> Others | |

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| teaching | | | |
| Necessary equipment and software | | | |
| Supporting people with special needs | | | |
| For technical support | | | |

Course learning outcomes (S= Skills, C= Competences K= Knowledge,)

| No. | Course learning outcomes | The associated program learning output code |
|--------------------|--|---|
| Knowledge | | |
| K1 | Define plane curves and space curves and their properties | MK 2 |
| K2 | Describe curvature and torsion and their geometric meanings | MK 2 |
| K3 | Characterize the different associated curves to a plane or a space curve. | MK 2 |
| K4 | Identify regular surfaces in the three dimension space | MK 1 |
| K5 | Perform the difference between the Euclidean distance and the distance on a surface, the role of the first fundamental form. | MK 2 |
| K6 | Identify the Gauss map, the second fundamental form. | MK 1 |
| K7 | Explain the Meaning of the Gauss's Theorem Egregium. | MK 1 |
| Skills | | |
| S1 | Draw the role of the second and third fundamental form of a surface. | MS 4 |
| S2 | Construct simple surfaces such as revolution surfaces, spheres, cylinder, ellipsoid... | MS 2 |
| S3 | Illustrate, using examples, minimal surfaces and surface of constant Gauss curvature. | MS 1 |
| S4 | Use concepts of differential geometry to diverse situations in physics, engineering or other mathematical contexts | MS 2 |
| Competences | | |
| C1 | Cooperate to work effectively in the group assignments. | MC 1 |
| | Solve different types of the important problems of geometry in everyday life. | MC 2 |

Mechanisms for direct evaluation of learning outcomes

| Type of assessment / learning style | Fully electronic learning | Blended learning | Traditional Learning (Theory Learning) | Traditional Learning (Practical Learning) |
|--|---------------------------|------------------|--|---|
| Midterm exam | 30% | 30% | 40% | 30% |
| Participation / practical applications | 0 | 0 | 10% | 30% |
| Asynchronous interactive activities | 30% | 20% | 0 | 0 |
| Final exam | 40% | 50% | 50% | 40% |

Schedule of simultaneous / face-to-face encounters and their topics

| Week | Subject | learning style* | Reference ** |
|------|---------|-----------------|--------------|
|------|---------|-----------------|--------------|

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| 1 | Plane and space curves | Lecture | 25-33 Ref 1 |
| 2 | Reparametrization by arc length, Curvature and Torsion, Applications. | Lecture | 35-49 Ref 1 |
| 3 | Frenet- Serret frame, Frenet- Serret Theorem. | Lecture | 50-81 Ref 1 |
| 4 | Osculating plane, Normal plane, Rectifying plane. | Lecture | 81-93 Ref 1 |
| 5 | Involutes, Evolutes, | Lecture | 95-100 Ref 1 |
| 6 | Bertrand curves, Spherical indicatrix. | Lecture | 116-127 Ref 1 |
| 7 | Global properties of curves, Simple closed curve. | Lecture | 127-139 Ref 1 |
| 8 | Isoperimetric inequality. Midexam | Lecture | 140-144 Ref 1 |
| 9 | Surfaces in three dimensions. | Lecture | 60-77 Ref 2 |
| 10 | Smooth surfaces. Examples of surfaces. | Lecture | 77-89 Ref 2 |
| 11 | The first fundamental form. Length of curves on surfaces | Lecture | 100-118 Ref 2 |
| 12 | Surface area. Propositions and examples. | Lecture | 118-126 Ref 2 |
| 13 | The second fundamental form. Gaussian formula. | Lecture | 139-148 Ref 2 |
| 14 | The normal and geodesic curvature, Principal curvatures. | Lecture | 148-153 Ref 2 |
| 15 | Mean and Gauss's curvatures. | Lecture | 153-158 Ref 2 |
| 16 | Final Exam | | |

Schedule of asynchronous interactive activities (in the case of e-learning and blended learning)

| Week | Task / activity | Reference | Expected results |
|------|---|--|------------------------------|
| 1 | Background | On vector valued functions and partial derivatives Students Notes or any Calculus book | Self-reading and Discussion |
| 2 | Video 1 Solving exercises | E-learning | Discussion in the class |
| 3 | Home work 1: On the subjects studied on the first three weeks | (Lecture notes and Ref.1) | Submit a pdf or word sheet |
| 4 | Quiz 1 | On the subjects studied on the first three weeks | Submitting on the E-learning |
| 5 | Assignment 1: On Frenet-Serret frame | Internet sources and the other Supportive learning resources | Presentation |
| 6 | Video 2 | Solving exercises | Discussion in the class |
| 7 | Home work 2 On the subjects studied in the weeks 4,5 and 6 | (Lecture notes and Ref.1) | Submit a pdf or word sheet |
| 8 | Assignment 2: On Bertrand curves | Internet sources and the other Supportive learning resources | Submitted with the mid exam |
| 9 | Self-reading | Surfaces in three dimensions. (Ref.2) | Talk |
| 10 | Video3 Solving exercises | E-learning | Discussion in the class |
| 11 | Home work 3: On the subjects studied after the midexam | (Lecture notes and Ref.1) | Submit a pdf or word sheet |
| 12 | Self-reading | Surface area (Ref.2) | Talk |
| 13 | Quiz 2 | On the subjects studied on the subject studied after midexam | Submitting on the E-learning |
| 14 | Presentation of the subject: The second fundamental form. | Internet sources and the reference book | Video |

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| 15 | Video 4 Revision of all the course | E-learning | |
| 16 | Final Exam | - | |