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| QF01/0408-4.0E | Course Plan for Master program - Study Plan Development and Updating Procedures/<br>Mathematics Department |
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|----------------|--|---|--|
| Study plan No. | 2021/2022  | University Specialization   | Master of Math.  |
| Course No.     | 0101711  | Course name   | Real Analysis  |
| Credit Hours   | 3  | Prerequisite/ Co-requisite  | None   |
| Course type    | <input type="checkbox"/> MANDATORY UNIVERSITY REQUIREMENT<br><input type="checkbox"/> UNIVERSITY ELECTIVE REQUIREMENTS | <input type="checkbox"/> FACULTY MANDATORY REQUIREMENT<br><input type="checkbox"/> Support course family requirements | <input checked="" type="checkbox"/> Mandatory requirements<br><input type="checkbox"/> Elective requirements |
| Teaching style | <input type="checkbox"/> Full online learning  | <input type="checkbox"/> Blended learning   | <input checked="" type="checkbox"/> Traditional learning   |
| Teaching model | <input type="checkbox"/> 1 Synchronous: 1 asynchronous   | <input type="checkbox"/> 2 face to face : 1 asynchronous  | <input checked="" type="checkbox"/> 2 Traditional  |

Faculty member and study divisions' information (to be filled in each semester by the subject instructor)

| Name            | Academic rank | Office No. | Phone No.          | E-mail         |                |
|-----------------|---------------|------------|--------------------|----------------|----------------|
|                 |               |            |                    |                |                |
|                 |               |            |                    |                |                |
| Division number | Time          | Place      | Number of students | Teaching style | Approved model |
|                 |               |            |                    |                |                |
|                 |               |            |                    |                |                |

Brief description

Riemann integral,  $\sigma$ -Algebra of Lebesgue, Outer measure, measurable sets and Lebesgue measure. Measurable functions. Lebesgue integral, integral of a nonnegative function, general Lebesgue integral, convergence in measure. Differentiation and integration, differentiation of monotone functions. The  $L^p$  spaces, Holder and Minkowski inequalities.

Learning resources

|   |   |                               |  |                                 |
|---|---|-------------------------------|--|---------------------------------|
| Course book information (Title, author, date of issue, publisher ... etc)                     | <ol style="list-style-type: none"> <li>1. Introduction to Real Analysis". By: R. Bartle and D. Sherbert. John Wiley &amp; Sons, Third Edition (2000).</li> <li>2. "Mathematical Analysis". By: T. Apostol Addison-Wesley Publishing Company, Second Edition (1974).</li> </ol>  |                               |  |                                 |
| Supportive learning resources (Books, databases, periodicals, software, applications, others) | <ol style="list-style-type: none"> <li>1. Introduction to Mathematical Analysis". By: S. Douglass Pearson, 3<sup>rd</sup> Edition (1996).</li> <li>2. "The Elements of Real Analysis". By: R. Bartle John Wiley &amp; Sons, 2<sup>nd</sup> Edition (1975).</li> <li>3. "Principals of Mathematical Analysis. By: W. Rudin McGraw Hill, 3<sup>rd</sup> Edition (1976)</li> </ol> |                               |  |                                 |
| Supporting websites   | <a href="https://en.wikipedia.org/wiki/Mathematical_analysis#Measure_theory">https://en.wikipedia.org/wiki/Mathematical_analysis#Measure_theory</a>   |                               |  |                                 |
| The physical environment for teaching   | <input checked="" type="checkbox"/> Class room  | <input type="checkbox"/> labs | <input checked="" type="checkbox"/> Virtual educational platform | <input type="checkbox"/> Others |
| Necessary equipment and software  |   |                               |  |                                 |
| Supporting people with special needs  |   |                               |  |                                 |
| For technical support   |   |                               |  |                                 |

Course learning outcomes (S= Skills, C= Competences K= Knowledge,)

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| No.                | Course learning outcomes  | The associated program learning output code |
|--------------------|---|---|
| <b>Knowledge</b>   |   |   |
| <b>K1</b>          | Apply the theorems of Riemann integral, $\sigma$ -Algebra of Lebesgue, Measurable Sets, and Measurable functions. | <b>MK 2</b>                                 |
| <b>K2</b>          | Understand the basic facts about Lebesgue Integral.   | <b>MK 1</b>                                 |
| <b>Skills</b>      |   |   |
| <b>S1</b>          | Recognize littlewood's three principles, Egoroff, Lusin, Lebesgue, and Jordan theorems.                           | <b>MS 2</b>                                 |
| <b>S2</b>          | Comprehend between Young, Holder and Minkowski inequalities.  | <b>MS 2</b>                                 |
| <b>Competences</b> |   |   |
| <b>C1</b>          | Cooperate to work effectively in the group assignments.   | <b>MC 1</b>                                 |
| <b>C2</b>          | Be able to think in mathematical analysis.  | <b>MC 2</b>                                 |

#### Mechanisms for direct evaluation of learning outcomes

| Type of assessment / learning style    | Fully electronic learning | Blended learning | Traditional Learning (Theory Learning) | Traditional Learning (Practical Learning) |
|--|---------------------------|------------------|--|---|
| Midterm exam                           | 30%                       | 30%              | 40%                                    | 30%                                       |
| Participation / practical applications | 0                         | 0                | 10%                                    | 30%                                       |
| Asynchronous interactive activities    | 30%                       | 30%              | 0                                      | 0   |
| Final exam                             | 40%                       | 40%              | 50%                                    | 40%                                       |

#### Schedule of simultaneous / face-to-face encounters and their topics

| Week | Subject   | learning style* | Reference ** |
|------|---|-----------------|--------------|
| 1    | Riemann integral  | Lecture         |              |
| 2    | The $\sigma$ -Algebra of Lebesgue Measurable Sets.<br>Four Characterizations for Measurable Sets.     | Lecture         |              |
| 3    | Outer and Inner Approximation of Lebesgue Measurable Sets.<br>Lebesgue Measure                        | Lecture         |              |
| 4    | Countable Additivity.<br>Non-measurable sets.<br>The Cantor Set and the Cantor-Lebesgue Function      | Lecture         |              |
| 5    | Lebesgue Measurable functions.<br>Sums, Products and Compositions.                                    | Lecture         |              |
| 6    | Littlewood's Three Principles,<br>Egoroff's Theorem, and Lusin's Theorem                              | Lecture         |              |
| 7    | Review of the Riemann Integral.<br>Simple Functions.<br>The Lebesgue Integral of a Bounded Measurable | Lecture         |              |
| 8    | Function over a Set of Finite Measure.  | Lecture         |              |

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|                | Properties of the integral.<br>Fatou's Lemma.   |         |  |
| 9              | Lebesgue Integral of a Measurable Nonnegative Function.<br>The General Lebesgue Integral.                         | Lecture |  |
| 10             | Countable Additivity and Continuity of Integration.<br>Uniform Integrability.                                     | Lecture |  |
| 11             | Continuity of Monotone Functions. Differentiability of Monotone Functions: Lebesgue Theorem. Functions of Bounded | Lecture |  |
| 12             | Jordan's Theorem.<br>Absolutely Continuous Functions.   | Lecture |  |
| 13             | Integrating Derivatives: Differentiating Indefinite Integrals.  | Lecture |  |
| 14             | $L^p$ Spaces.<br>Inequalities of Young.   | Lecture |  |
| 15             | Inequalities of Holder and Minkowski.   | Lecture |  |
| 16             | <b>Final Exam Midterm exam</b>  |         |  |

### Schedule of asynchronous interactive activities (in the case of e-learning and blended learning)

| Week | Task / activity   | Reference   | Expected results             |
|------|---|---|------------------------------|
| 1    | Background  | Real Analysis 1   | Self-reading and Discussion  |
| 2    | Video 1 Solving exercises                                     | E-learning  | Discussion in the class      |
| 3    | Home work 1: On the subjects studied on the first three weeks | (Lecture notes and Ref.1)   | Submit a pdf or word sheet   |
| 4    | Quiz 1  | On the subjects studied on the first three weeks                  | Submitting on the E-learning |
| 5    | Assignment 1  | Internet sources and the other Supportive learning resources      | Presentation                 |
| 6    | Video 2   | Solving exercises   | Discussion in the class      |
| 7    | Home work 2 On the subjects studied in the weeks 4,5 and 6    | (Lecture notes and Ref.1)   | Submit a pdf or word sheet   |
| 8    | Assignment 2  | Internet sources and the other Supportive learning resources      | Submitted with the mid exam  |
| 9    | Self-reading for selected topic                               | (Ref.2)   | Talk                         |
| 10   | Video3 Solving exercises                                      | E-learning  | Discussion in the class      |
| 11   | Home work 3: On the subjects studied after the Midterm exam   | (Lecture notes and Ref.1)   | Submit a pdf or word sheet   |
| 12   | Self-reading for selected topic                               | (Ref.2)   | Talk                         |
| 13   | Quiz 2  | On the subjects studied on the subject studied after Midterm exam | Submitting on the E-learning |
| 14   | Presentation of the selected subject                          | Internet sources and the reference book                           | Video                        |

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| 15             | Video 4 Revision of all the course | E-learning   |  |
| 16             | <b>Final Exam</b>                  | -  |  |